

Roll No

MCTA-102**M.E/M.Tech., I Semester**

Examination, December 2014

Programming System*Time : Three Hours**Maximum Marks : 70**Note:* Attempt any five questions. All questions carry equal marks.

1. a) Let $A = \{7, 2, 4, 17, 1, 11, 68, 15, 10, 20\}$. Draw a binomial Heap whose keys are elements of A. And insert a new element with key 5 into this Heap? 7
- b) What is the height of a B-Tree, if there are n nodes in it? What is the maximum height of a B-Tree with 10,00,000 keys and having minimum degree 10? 7
2. Explain the Master theorem and solve the following: 14
 - i) $T(n) = T(\sqrt{n}) + 1$
 - ii) $T(n) = 2T(n/4) + \sqrt{n}$
 - iii) $T(n) = 2T(n^2) + n^2$
3. a) Apply Backtracking techniques to solve the following instance of the subset sum problem. 7
 $[S = (1, 3, 4, 5) \text{ and } d = 11]$

- b) What are the two different types of recurrence? Solve the recurrence relation $T(n) = 3T\left(n^{1/3}\right) + \log 3^n$. 7

4. Discusses the classes P, NP, NP complete and NP Hard with examples. How can we show that a problem is NP Complete? 14
5. Explain following Term: 14
 - i) Set algorithms
 - ii) Hard problems
 - iii) Combinatorial Algorithm
6. a) Explain in detail about Approximation algorithm for NP Hard problem with example. 7
- b) Discuss Travelling salesman problem with help of suitable example? 7
7. a) Assume that $m = 30$ and $n = 3$. While weights are (10, 20, 30) and profits are (12, 20, 24) then find the optimal solution using knap-sack techniques? 7
- b) Discuss the best, worst, average case efficiency of Binary Search Algorithm? 7
8. Write a short notes (Any Four): 14

a) Priority queues	b) Internal sorting
c) Hash functions	d) Radix sort
e) Space complexity	f) Dynamic programming.