

[4]

b) Evaluate by using Laplace transform

i) $\int_0^\infty t e^{-At} \sin t dt$

ii) $\int_0^\infty e^{-t} \frac{\sin t}{t} dt$

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Total No. of Questions : 8]

[Total No. of Printed Pages : 4

Roll No

BE-3001 (CS/IT) (CBGS)

B.E., III Semester

Examination, December 2017

Choice Based Grading System (CBGS)

Mathematics - III

Time : Three Hours

Maximum Marks : 70

- Note:* i) Attempt any five questions.
 ii) All questions carry equal marks.

1. a) Prove that

$$x^2 = \frac{\pi^2}{3} + 4 \sum_{n=1}^{\infty} (-1)^n \frac{\cos nx}{n^2}, \quad -\pi < x < \pi$$

Hence show that $\sum \frac{1}{n^2} = \frac{\pi^2}{6}$

b) Obtain half-range sine series for e^x in $0 < x < 1$

2. a) Find the Fourier transform of $f(x) = \begin{cases} 1-x^2, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases}$

Hence evaluate $\int_0^\infty \frac{x \cos x - \sin x}{x^3} \cos \frac{x}{2} dx$

- b) Using Laplace transform to solve the diff. equation

$$\frac{d^2x}{dt^2} - 2\frac{dx}{dt} + x = e^t$$

When $x = 2$, $\frac{dx}{dt} = -1$ at $t = 0$

3. a) Find the Laplace transform of $\frac{1 - \cos t}{t^2}$

- b) Using the convolution theorem, find

$$L^{-1} \left\{ \frac{s}{(s^2 + 1)(s^2 + 4)} \right\}$$

4. a) Define:

i) Probability density function for continuous random variables.

ii) Mean and variance of random variables.

- b) Find the mean and variance for Binomial distribution.

5. a) Fit Poisson's distribution to the following and calculate theoretical frequencies ($e^{-0.5} = 0.61$)

Deaths: 0 1 2 3 4

Frequency: 122 60 15 2 1

- b) Show that the mean deviation from the mean of the normal

distribution is $\frac{4}{5}$ times its standard deviation.

6. a) By the method of least squares. Find the straight line that best fits the following data:

x	1	2	3	4	5
y	14	27	40	55	68

- b) The profit of certain company in the x^{th} year of its life are given by:

x	1	2	3	4	5
y	1250	1400	1650	1950	2300

Taking $u = x - 3$ and $50v = y - 1650$, show that the parabola of second degree of y on x is

$$y = 1140.05 + 72.1x + 32.15x^2.$$

7. a) Find the Fourier series for $f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ x, & 0 < x < \pi \end{cases}$

and deduce that $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$

- b) Find the Fourier cosine transform of $f(x) = \frac{1}{1+x^2}$ and

hence find Fourier sine transform of $F(x) = \frac{x}{1+x^2}$

8. a) For a Poisson distribution with mean m , show that

$$\mu_{r+1} = m r \mu_{r-1} + m \frac{d\mu_r}{dm}$$

$$\text{Where } \mu_r = \sum_{x=0}^{\infty} (x-m)^r e^{-m} \frac{m^x}{x!}$$