

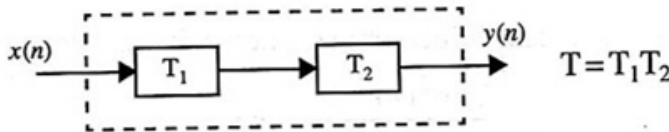
Roll No .....

**MEDC-103**  
**M.E./M.Tech., I Semester**  
**Examination, June 2016**  
**DSP Application**  
**Time : Three Hours**

**Maximum Marks : 70**

- Note:** i) Attempt all questions.  
ii) All questions carry equal marks.  
iii) Attempt any two parts from each questions.

1. a) Two discrete - time systems  $T_1$  and  $T_2$  are connected in cascade to form a new system  $T$  as shown in figure. If  $T_1$  and  $T_2$  are LTI, test whether interchanging the orders of  $T_1$  and  $T_2$  does not change the system  $T$ .



- b) The discrete - time system  
 $y(n) = ny(n-1) + x(n) \quad n \geq 0$   
is at rest [i.e.  $y(-1) = 0$ ]. Check if the system is linear time invariant and BIBO stable.
- c) Determine the zero - input response of the system described by the second - order difference equation.  
 $x(n) - 3y(n-1) - 4y(n-2) = 0$
2. a) Determine one-sided Z-transform of  
 $y(n) + 0.5y(n-1) - 0.25y(n-2) = 0$   
given that  $y(-1) = y(-2) = 1$
- b) State and prove the following properties of Z-transform :  
i) Time shifting      ii) Differentiation

- c) Determine the inverse of Z-transform of causal

$$X(z) = \frac{4 - 8z^{-1} + 6z^{-2}}{(1 - 2z^{-1})^2(1 + z^{-1})}$$

3. a) State and prove shifting property of DFT.  
b) Find the convolution of the two signals

$$x(n) = 3^n u(-n); \quad h(n) = \left(\frac{1}{3}\right)^n u(n-2)$$

- c) How do you linear filtering by FFT using save-add method.

4. a) Obtain the Direct form II

$$y(n) = -0.1(n-1) + 0.72y(n-2) + 0.7x(n) - 0.252x(n-2)$$

- b) Convert the analog filter  $H(s) = \frac{0.5(s+4)}{(s+1)(s+2)}$  using

impulse invariant transformation  $T = 0.31416s$ .

- c) Write the characteristics features of Hanning window.

5. a) An ideal Hilbert transformer with impulse response

$$h[n] = \begin{cases} \frac{2 \sin^2(\pi n / 2)}{\pi n}, & n \neq 0, \\ 0, & n = 0, \end{cases}$$

has input  $x_r[n]$  and output  $x_i[n] = x_r[n] * h[n]$ , where  $x_r[n]$  is a discrete-time random signal. Find an expression for the cross-correlation sequence  $\Phi_{x_r x_i}[m]$ . Show that in this case  $\Phi_{x_r x_i}[m]$  is an odd function of  $m$ .

- b) Write short note on spectrum estimation.  
c) Explain how power spectrum can be estimated from the AR model.

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